

Homework 1: Structure of the blockchain and how cryptography plays a role

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Abstract. We'll focus on the blockchain as a data structure to understand how cryptography provides a role to self-enforce its integrity. Next we'll look at how the database is structured in Bitcoin (UTXO model) and Ethereum (Account-based model), and how transactions are processed to update the database. It is recommended to make notes on this homework sheet for future use.

1 Cypherpunks write code

Before deep-diving into the blockchain's structure, it's worth taking a step back to understand the motivation for why something like Bitcoin even exists. On several occasions, Satoshi Nakamoto made it clear that Bitcoin emerged due to the mis-trust of banks and the lack of transparency in the global financial system:

The root problem with conventional currency is all the trust that's required to make it work. The central bank must be trusted not to debase the currency, but the history of fiat currencies is full of breaches of that trust. Banks must be trusted to hold our money and transfer it electronically, but they lend it out in waves of credit bubbles with barely a fraction in reserve. We have to trust them with our privacy, trust them not to let identity thieves drain our accounts. - Satoshi Nakamoto

Remember, the bitcoin whitepaper was first posted on the 31st October 2008 and the running code was later published on the 3rd January 2009. Satoshi Nakamoto was clearly working on Bitcoin during the Great Financial Crisis that was sparked due to the sub-prime mortgage crisis. The banks were at the heart of this crisis as they sold mortgages to people with bad credit ratings with the expectation that if the price of houses kept going up, then both parties could profit. When the housing market's bubble burst in 2006, it triggered defaults as the initial loans were worth more than the purchased house. The toxic loans and risk spread throughout the markets (i.e. securities, pension funds, etc) and eventually nearly took them down. As Satoshi Nakamoto highlighted, this was all possible because banks could lend more money than they held in deposits, and they had full custody over all deposits. Even worse and to Satoshi Nakamoto's frustration, the banks *got away with it* as national governments bailed them out:

The Times 03/Jan/2009 Chancellor on brink of second bailout for banks. -
Genesis Block

Satoshi Nakamoto was clearly versed in the Cypherpunk's Manifesto¹ which at its heart focuses on how cryptography can be used to remove power-imbalances in society. We can speculate that during the financial crisis, Satoshi Nakamoto was trying to work out how cryptography can be used to build a global currency that empowers the individual, and not any single nation state. On hindsight (and in spite of 30+ years research), Satoshi Nakamoto was the first to investigate how to build a peer-to-peer electronic cash system without the support of a central authority/currency issuer. This eventually led to the *blockchain* which is a cryptographic audit log that lets anyone re-compute the contents of a database and *Nakamoto Consensus* that lets financially motivated peers compete to update the database (and thus remove the need for any appointed authority).

For this homework, we'll solely focus on how cryptography provides integrity to the blockchain, how the database is structured and how transactions are processed.

2 Two Cryptographic Primitives

While Bitcoin, Ethereum and their derivatives are called *cryptocurrencies*, at heart they are built upon two basic cryptographic primitives.

2.1 Cryptographic Hash Functions

First let's cover the basic idea of a hash function before we explore how it is used in a cryptocurrency.

- What is a hash function? [2 marks]
- Identify and explain the three properties that make a hash function cryptographic? [6 marks]

Good job! Let's now cover how a cryptographic hash function is used in Bitcoin to support *simplified payment verification* for light clients.

- What is a merkle tree and a merkle tree root? [2 marks]
- How are the blocks chained together to form the blockchain? [2 marks]
- What information is required to prove a transaction is in a block? And how does a light client verify it? [6 marks]
- Why does simplified payment verification have weaker security guarantees compared to processing the entire blockchain? [4 marks]

¹ <https://www.activism.net/cypherpunk/manifesto.html>

2.2 Digital Signatures

Next we need to consider how users can register to use a cryptocurrency and how they can prove they are entitled to spend their new coins.

- What is a digital signature? And what digital signature algorithm is typically used in cryptocurrencies? [4 marks] w
- Why is it important to always use fresh randomness when computing a digital signature? [2 marks]

3 Database Structure

The blockchain's only purpose is to let anyone re-execute all transactions in sequential order to re-compute a database. In class, we tried to focus on the database's structure for both Bitcoin and Ethereum:

- Bitcoin's database follows a UTXO model as the ledger simply consists of a list of unspent transaction outputs.
- Ethereum's database follows an Account-based model where the ledger records the current balance, storage and nonce for every account.

Let's take this opportunity to assess our understanding of the blockchain's structure. To begin, we'll focus on Bitcoin:

- What is the role of an input and output in a Bitcoin transaction? And why is there no real concept of a coin? [4 marks]
- Name three typical spending conditions that is supported in Bitcoin. [3 marks]
- What is the UTXO set? [2 marks]
- When the wallet software processes a transaction inside a block, how is the UTXO set updated? [4 marks]
- Let's pretend 10 transactions are accepted into a block, and each transaction has an output that sends 1 coin to the bitcoin address A . How many entries in the UTXO set will be recorded and why? [2 marks]
- Why is it difficult to assume that if a transaction is spending two or more sets of coins, then they all belong to the same user? [4 marks]

The UTXO model is popular for its simplicity, its statelessness, and its determinism. Except for some quirks, it works great for processing financial transactions and supporting obfuscation of ownership. However it has so far proven difficult for designing fair-exchange protocols that run on top of Bitcoin which eventually led to the development of Ethereum's account-based model.² Let's explore some questions around it:

- What information is stored for each account? [5 marks]

² A long running joke is that designing a new protocol in Bitcoin can get you a top-tier Oakland publication, whereas the same protocol in Ethereum gets you a blog post.

- What is a replay attack? And why does the transaction nonce stop it? [4 marks]
- When processing an Ethereum transaction that interacts with a contract, what basic validation checks are performed on the transaction and how does the software update the account database? [6 marks]

For the final question let's discuss:

- What are the subtle differences between Bitcoin's UTXO model and Ethereum's account-based model? [8 marks]

While the answers will be released in a week's time, if you found any of the questions difficult then please visit Patrick McCorry during his office hours.